Blind Source Separation of Acoustic Signals Based on Multistage Independent Component Analysis

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ABSTRACT

We propose a new algorithm for blind source separation (BSS), in which frequency-domain independent component analysis (FDICA) and time-domain ICA (TDICA) are combined to achieve a superior source-separation performance under reverberant conditions. Generally speaking, conventional TDICA fails to separate source signals under heavily reverberant conditions because of the low convergence in the iterative learning of the inverse of the mixing system. On the other hand, the separation performance of conventional FDICA also degrades significantly because the independence assumption of narrow-band signals collapses when the number of subbands increases. In the proposed method, the separated signals of FDICA are regarded as the input signals for TDICA, and we can remove the residual crosstalk components of FDICA by using TDICA. The experimental results obtained under the reverberant condition reveal that the separation performance of the proposed method is superior to that of conventional ICA-based BSS methods.

1 Introduction

Source separation of acoustic signals is to estimate the original sound source signals from among the mixed signals observed in each input channel. This technique is applicable to the realization of noise-robust speech recognition and high-quality hands-free telecommunication systems. The methods of achieving the source separation can be classified into two groups: methods based on a single-channel input, and those based on multichannel inputs. As single-channel types of source separation, a method of tracking a formant structure [1], the organization technique for hierarchical perceptual sounds [2], and a method based on auditory scene analysis [3] have been proposed. As multichannel-type source separation, the method based on array signal processing, e.g., a microphone array system, is one of the most effective techniques [4]. In this system, the directions of arrival (DOAs) of the sound sources are estimated and then each of the source signals is separately obtained using the directivity of the array. The delay-and-sum array and the adaptive beamformer are conventional and popular microphone arrays currently used for source separation and noise reduction.

In recent years, alternative source-separation approaches have been proposed by researchers using not array signal processing but a specialized branch of information theory, i.e., information-geometry theory [5, 6]. Blind source separation (BSS) is the approach for estimating original source signals using only the information of the mixed signals observed in each input channel, where the independence among the source signals is mainly used for the separation. This technique is based on unsupervised adaptive filtering [6], and provides us with extended flexibility in that the source-separation procedure requires no training sequences and no a priori information on the DOAs of the sound sources. The early contributory works on BSS were performed by Cardoso and Jutten [7, 8], where high-order statistics of the signals are used for measuring the independence. Common has clearly defined the term independent component analysis (ICA), and presented an algorithm that measures independence among the source signals [9]. This report on ICA was later followed by Bell and Sejnowski, where ICA extended to the informax (or the maximum-entropy) algorithm for BSS which is based on a minimization of mutual information of the signals [10].

The BSS methods based on ICA [9, 10] can be classified into two groups in terms of the processing domain, i.e., frequency-domain ICA (FDICA) in which the complex-valued inverse of the mixing matrix is calculated in the frequency domain [11, 12, 13], and time-domain ICA (TDICA) in which the inverse system of the mixing FIR-filter matrix is calculated in the time domain [5, 14]. The recently developed BSS techniques can achieve a good source-separation performance under artificial or short reverberant conditions. However, the performances of these methods under heavily reverberant conditions significantly degrade because of the following problems. (1) In conventional FDICA, the source-separation performance is saturated before reaching a sufficient performance because we transform the fullband signals into the narrow-band signals and the independence assumption collapses in each narrow-band [15]. (2) In TDICA, the convergence degrades because the iterative learning rule becomes more complicated as the reverberation increases.

In order to resolve the above problems, we propose a new BSS algorithm called multistage ICA (MSICA), in which FDICA and TDICA are combined. By using the proposed method, we can achieve a superior source-separation performance even under heavily reverberant conditions. The results of the signal separation experiments reveal that the signal-separation performance of the proposed algorithm is superior to those of conventional ICA-based BSS methods.

The rest of this paper is organized as follows. In Section 2, the sound mixing model of the microphone array is explained. In Section 3, conventional ICA and its problems
Advantages: disadvantage.

Advantages of the mixing matrix $A(f)$ in each subband, and (3) recon­
nals into the narrow-band signals, (2) optimize the inverse

3.1 Frequency-Domain ICA

The conventional BSS based on FDICA is conducted with the following steps: (1) transform the observed fullband sig­

Advantages:

(F1) We can simplify the convolutive mixture down to si­
multaneous mixtures by the frequency transform.

(F2) It is easy to converge the separation filter in iterative

Disadvantages:

(F3) The separation performance is saturated before reach­ing a sufficient performance because the independence

assumption collapses in each narrow-band [15] (see, e.g.,

Sect. 5.2).

(F4) Permutation among source signals and indeterminacy

of each source gain in each subband.

As for disadvantage (F4), various solutions have already been

proposed [11, 16, 17, 18]. However, the collapse of the inde­

pendence assumption, (F3), is a serious and inherent prob­

lem, and this prevents us from applying FDICA in a real

acoustic environment with a long reverberation.

3.2 Time-Domain ICA

In the conventional BSS based on TDICA, each element of

the mixing matrix is represented as a FIR filter. We can

optimize its inverse, i.e., form an inverse filter system, by

using the fullband observed signals themselves. TDICA has

the following advantages and disadvantages.

Advantages:

(T1) We can treat the fullband speech signals where the

independence assumption of sources usually holds.

(T2) High-convergence possibility near the optimal point.

Disadvantages:

(T3) The iterative rule for FIR-filter learning is compli­
cated.

(T4) The convergence degrades under reverberant condi­tions.

It is known that TDICA works only in the case of mixtures

with a short-tap FIR filter, i.e., less than 100 taps. Also,

TDICA fails to separate source signals under real acoustic

environments because of disadvantages (T3) and (T4).

4 Proposed Method: Multistage ICA [19, 20]

As described above, the conventional ICA methods have

some disadvantages. However, note that the advantages and

disadvantages of FDICA and TDICA are mutually comple­

mentary, i.e., (F3) can be resolved by (T1) and (T2), and

(T3) and (T4) can be resolved by (F1) and (F2). Hence, in

order to resolve the disadvantages, we propose a new algo­

rithm, MSICA, in which FDICA and TDICA are combined

(see Fig. 2).

MSICA is conducted with the following steps. In the first

stage, we perform FDICA to separate the source signals to

some extent with the high-stability advantages of FDICA,

(F1) and (F2). In the second stage, we regard the separated

signals of FDICA as the input signals for TDICA, and we

remove the residual crosstalk components of FDICA by using

TDICA. Finally, we regard the output signals of TDICA as

the resultant separated signals. MSICA can achieve a high

stability and a separation performance superior to that of

conventional FDICA and TDICA. In the following sections,

we describe details of the ICA-learning rules for each stage.

4.1 First-Stage ICA: Frequency-Domain ICA

In the first-stage ICA, we introduce the fast-convergence

FDICA proposed by one of the authors [13]. We perform the

signal separation procedure as described below (see FDICA

in Fig. 2).
In FDICA, first, the short-time analysis of observed signals is conducted by frame-by-frame discrete Fourier transform (DFT). By plotting the spectral values in a frequency bin of each microphone input frame by frame, we consider them as a time series. Hereafter, we designate the time series as $X(f, t) = [X_1(f, t), \ldots, X_K(f, t)]^T$. Next, we perform signal separation using the complex-valued inverse of the mixing matrix, $W'(f)$, so that the $L$ time-series output $Y'(f, t) = [Y'_1(f, t), \ldots, Y'_L(f, t)]^T$ becomes mutually independent; this procedure can be given as
\[
Y'(f, t) = W'(f)X(f, t).
\]

We perform this procedure with respect to all frequency bins. Finally, by applying the inverse DFT and the overlap-add technique to the separated time series $Y'(f, t)$, we reconstruct the resultant source signals in the time domain, $y'(t)$.

In conventional FDICA, the optimal $W'(f)$ is obtained by the following iterative equation [11]:
\[
W'(f) = W'(f) + \eta \left[ \text{diag} \left( \Phi(Y'(f, t))Y'(f, t)^H \right) \right],
\]

where $(\cdot)_s$ denotes the time-averaging operator, $\eta$ is used to express the value of the $s$-th step in the iterations, and $\eta$ is the step-size parameter. Also, we define the nonlinear vector function $\Phi(\cdot)$ as
\[
\Phi(Y'(f, t)) = \begin{bmatrix} \Phi(Y'_1(f, t)), \ldots, \Phi(Y'_L(f, t)) \end{bmatrix}^T,
\]
where $\Phi(\cdot)$ denotes the complex-valued inverse of the mixing matrix, and $\Phi(\cdot)$ denotes the time-averaging operator for the $s$-th local analysis block.

4.2 Second-Stage ICA: Time-Domain ICA

In the second-stage ICA, we introduce the TDICA which uses nonstationarity of the source signals (see TDICA in Fig. 2). We separate the sources by minimizing the non-negative cost function which takes the minimum value only when the second-order cross-correlation becomes zero if the source signals are nonstationary. The cost function can be given as [14]
\[
Q(W'(f)) = \frac{1}{2B} \sum_{b=1}^{B} \left\{ \text{det} R_b'(0) \right\},
\]

where $B$ is the number of local analysis blocks. $R_b'(0)$ is the correlation matrix of the separated signals, i.e., $R_b'(0) = \langle y(l) y((t-n)) \rangle_b$, where $\langle \cdot \rangle_b$ denotes the time-averaging operator for the $b$-th local analysis block, $y(l)$ is the resultant separated signal vector, and $W'(f)$ is the $z$-transform of the separation filter coefficient $w_b'(n)$ ($n = 0, \ldots, N - 1$); these are given as
\[
y(t) = [y_1(t), \ldots, y_L(t)]^T = W'(z) \cdot y'(t),
\]
\[
W'(z) = \sum_{n=0}^{N-1} w_b'(n) z^{-n},
\]

where $z^{-1}$ is used as the unit-delay operator for convenience, i.e., $z^{-n} \cdot x(t) = x(t - n)$, and $y_b'(t)$ is the time-domain output of FDICA.

Equation (9) becomes zero only when $y_b'(t)$ and $y_L'(t)$ are uncorrelated for all of the local analysis blocks. Calculating the natural gradient [21] of $Q(W'(z))$, we obtain the iterative equation of the separation filter $w_b'(n)$ to minimize Eq. (9) as [19]
\[
w_{b+1}'(n) = w_{b}'(n) - \frac{\alpha}{B} \frac{\partial Q(W_{b}'(z))}{\partial w_{b}'(n)} W_{b}'(z) W_{b}'(z)^T
\]
\[
= w_{b}'(n) + \frac{\alpha}{B} \sum_{b=1}^{B} \left( \text{diag} R_b'(0) \right)^{-1} R_b'(0) W_{b}'(z),
\]

where $\alpha$ is the step-size parameter. Equation (12) evaluates only off-diagonal of $R_b'(0)$, and we note that this is not sufficient for the separation under heavily reverberant conditions [19]. Therefore we expand Eq. (12) to the following
Figure 3: Layout of reverberant room used in experiments.

and the independence assumption collapses in each frequency band, particularly when the number of subbands is large.

In order to confirm the fact, we newly define the following objective measure to quantify an independence, and investigate the relation between the number of subbands and the independence among subband signals.

\[ J = \left( \begin{array}{c} \text{diag} \left( \Phi(Y(f,t))Y^{H}(f,t) \right) \text{diag} \left( \Phi^{*}(Y(f,t))Y^{H}(f,t) \right) \end{array} \right) \]

where \( \| \cdot \| \) is frobenius norm of matrix. This measure \( J \) is a part of the iterative equation (6). If narrow-band signals become mutually independent, the measure \( J \) becomes zero. Also we can consider that the independence of subband signals is high when \( J \) is small. In order to evaluate the independence of real narrow-band speech signals, we carried out the experiment in which the input signal, \( Y(f,t) \), in Eq. (14) is regarded as the perfectly separated sources, i.e., original speech samples. Figure 5 shows the relation between the number of subbands and the value of \( J \) which corresponds to the independence of subband signals. Figure 5 shows that the independence decreases as the number of subbands increases, especially when the number of subbands is large.

Above-mentioned experimental results clarify the disadvantage that the separation performance is saturated in FDICA because we transform the fullband signals into the narrow-band signals. We should lengthen the separation filter (or FFT length for analysis) when we confront with a long reverberation. In this case, however, the independence of subband signals decreases. Thus, there is a trade-off relation among the independence of subband signals and robustness against reverberation as shown in Figure 6. On the basis of these results, we should cascade another signal processing analysis, e.g., TDICA, with FDICA to obtain the further separation performances.

5.3 Relation between Separation Performance and Filter Length in TDICA

We carried out the experiments using TDICA and MSICA to evaluate the contribution of increments of separation-filter length for improving the separation performances under reverberant conditions. The analysis conditions of these experiments are as follows: the filter length \( N \) is set to be from 10 to 2000 taps, the maximum number of iterations is 500,
Figure 5: Relation between the number of subbands and the value of $J$ defined by Eq. (14), which corresponds to the independence of subband signals.

Figure 6: Trade-off relation among the independence of subband signals and robustness against reverberation.

Figure 7: Relation between separation performance and filter length in (a) TDICA and (b) TDICA part in MSICA.

and the step-size parameter $\alpha$ for iterations is set to be $1/N$. As for the local analysis block, we divided the signals equally into $B$ parts ($B = 1 \sim 10$). We chose the optimal $B$ and number of iterations for each filter length because the convergence is different for every filter length. As for the FDI CA part in MSICA, the analysis conditions are the same as those given in Sect. 5.2, except for the number of subbands (which is fixed at 1024 bands).

Figures 7(a) and (b) show the NRR results in the conventional TDICA and MSICA for different filter lengths. As shown in Fig. 7(a), when the separation filter is lengthened, the separation performance of the TDICA degrades. This also implies that the simple TDICA separates only the direct components of arriving signals. On the other hand, in Fig. 7(b), the separation performance of MSICA is improved when the filter length is longer. This reveals that the TDICA part in MSICA can separate the source signals even with the reverberation components, and the TDICA is still useful near the optimal point.

5.4 Comparison between Conventional ICA and MSICA

We compared the performance of the proposed MSICA with that of the conventional ICA under the reverberant condition. As for FDI CA, the analysis conditions are the same as those given in Sect. 5.2, except for the number of subbands (which is fixed at 1024 bands). As for the conventional TDICA, the number of local analysis blocks, $B$, is fixed at 3 blocks, the number of iterations is 400, and the filter length is 10 taps. As for the TDICA part in MSICA, the number of local analysis blocks, $B$, is fixed at 9 blocks, the number of iterations is 400, and the filter length is 1000 taps.

Figure 8 shows the NRRs of the conventional FDI CA, conventional TDICA, and MSICA. In this figure, we separately plot the NRRs for different combination of speakers, and the averages of their NRRs. The results reveal that the separation performances of the proposed MSICA are superior to those of the conventional FDI CA and TDICA with every combination. Specifically, compared with the conventional ICA, the proposed method can improve the NRR by about 2.7 dB over that of FDI CA and by about 6.2 dB over that of TDICA, for an average of 12 combinations.

As described in Sect. 5.2, the FDI CA in this study showed the saturation of NRR when we used the 1024-subband analysis. As described in Sect. 5.3, the simple TDICA could not separate the source signals accurately under the reverberant condition. These findings indicate the practical limitations of the separation performances of conventional ICA-based BSS methods. From the results of Fig. 8, however, we can confirm that the proposed MSICA can inherently remove these limitations, and is effective for improving the separation performance and convergence under reverberant conditions.

6 Conclusion

In this paper, we propose a new algorithm for BSS, in which FDI CA and TDICA are combined to achieve a superior source-separation performance under reverberant conditions. The results of the signal separation experiments reveal that the separation performance of the proposed algorithm is su-
Figure 8: Comparison of noise reduction rates obtained by MSICA, conventional FDICA and the conventional TDICA.

Figure 8: Comparison of noise reduction rates obtained by MSICA, conventional FDICA and the conventional TDICA.

prior to that of conventional ICA-based BSS methods, and the combination of FDICA and TDICA is inherently effective for improving the separation performance. Specifically, the proposed method can improve the SNR by about 2.7 dB over that of FDICA and by about 6.2 dB over that of TDICA, for an average of 12 speaker-combinations.

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